# Structure, Spectra, and Reaction Energies of the Aluminum-Phosphorus Rings (HAI-PH) $\mathbf{2}^{2}$ and $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ and the $(\mathbf{H A I}-\mathbf{P H})_{4}$ Cluster 

Randall D. Davy<br>Department of Chemistry, Liberty University, Lynchburg, Virginia 24502<br>Henry F. Schaefer, III*<br>Center for Computational Quantum Chemistry, University of Georgia, Athens, Georgia 30602

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#### Abstract

Recently a six-membered ring consisting of three coordinate aluminum and phosphorus was synthesized, as well as an $\mathrm{R}_{2} \mathrm{AlPR}^{\prime}{ }_{2}$ compound of three coordinate aluminum and phosphorus. This research was initiated in order to better understanding the bonding in these new compounds, as well as the more common compounds that contain four coordinate aluminum and phosphorus. Ab initio investigations of the structure, bonding, vibrational spectra, and reaction energies for the unknown three coordinate ring $(\mathrm{HAl}-\mathrm{PH})_{2}$, the four coordinate ring $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$, and the four coordinate cluster $(\mathrm{HAl}-\mathrm{PH})_{4}$ are presented. The three coordinate ring has two conformers that are within $3 \mathrm{kcal} \mathrm{mol}^{-1}$ in energy. The higher energy conformer is planar and the $\mathrm{P}-\mathrm{H}$ bonds are trans, while the other is puckered and the $\mathrm{P}-\mathrm{H}$ bonds are cis. The theoretical $\mathrm{Al}-\mathrm{P}$ bond lengths are within $0.01 \AA$ of the experimental values for the three coordinate $\mathrm{Al}-\mathrm{P}$ compounds, despite the size difference between the hydrogen atoms of the model compound and the substituents on the experimentally determined structures. The structures for $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ and for the $(\mathrm{HAl}-\mathrm{PH})_{4}$ cube are also in good agreement with analogous known compounds. The theoretical energies of $\mathrm{H}_{2}$ loss and dimerization to form the cube compound from an initial Lewis acid-base adduct are also reported. The laboratory synthesis of (RAl$\left.\mathrm{PR}^{\prime}\right)_{2}$ compounds should be possible.


## Introduction

In their synthesis of the cubic cluster $\left(\mathrm{RAl}-\mathrm{PR}^{\prime}\right)_{4}(\mathrm{R}=\mathrm{iBu}$, $\mathrm{R}^{\prime}=\mathrm{Ph}_{3} \mathrm{Si}$ ), Cowley, Jones, Mardones, Atwood, and Bott begin with $\mathrm{iBu}_{2} \mathrm{AlH}$ and $\mathrm{Ph}_{3} \mathrm{SiPH}_{2} .{ }^{1}$ The reaction proceeds through elimination of hydrogen to form a ring of formula ( $\mathrm{R}_{2} \mathrm{Al}-$ $\left.P^{\prime} R^{\prime}\right)_{2}$. This initial ring undergoes elimination of isobutane and forms the cube. Although a mechanism has not been proposed, it is possible that an intermediate ( $\left.\mathrm{RAl}-\mathrm{PR}^{\prime}\right)_{2}$ ring, which has phosphorus and aluminum atoms that are only three coordinate, is formed. Such a ring has not yet been synthesized. Recently a six-membered-ring compound with three coordinate aluminum and phosphorus was synthesized by Wehmschulte and Power. ${ }^{2}$ This was only the second compound with a bond between three coordinate aluminum and phosphorus to be structurally characterized. The other was the $\left(2,4,6-(i \operatorname{Pr})_{3} \mathrm{C}_{6} \mathrm{H}_{2}\right)_{2}-$ $\mathrm{Al}-\mathrm{P}(1$-adamantyl $)\left(\mathrm{SiPh}_{3}\right)$ compound reported by Wehmschulte, Ruhlandt-Senge, and Power. ${ }^{3}$ Although the chemistry of aluminum phosphorus compounds has been reviewed by Haaland as a part of aluminum coordination chemistry, ${ }^{4}$ this was prior to synthesis of any three coordinate $\mathrm{Al}-\mathrm{P}$ compounds. Haaland used the Schomaker-Stevenson rule to predict the $\mathrm{Al}-\mathrm{P}$ bond length between three coordinate Al and P atoms to be $2.31 \AA$. The $\mathrm{Al}-\mathrm{P}$ bonds in the two compounds now known are 2.328 (3) $\AA$ for the six-membered ring $^{2}$ and $2.342 \AA$ for the unassociated compound. ${ }^{3}$

Both of the recently synthesized compounds have of necessity sterically demanding substituents. Theoretical model compounds have the advantage of eliminating the complicating factors of sterically demanding substituents that could alter bond lengths and angles. Trends in bond lengths and angles obtained will ordinarily be due only to underlying bonding considerations. Recently reviews of low-valent phosphorus-boron compounds

[^0]have been published, ${ }^{5-7}$ and low-valent $\mathrm{Al}-\mathrm{N}$ compounds have been studied. ${ }^{8,9}$ To date the only theoretical studies of lowvalent $\mathrm{Al}-\mathrm{P}$ compounds have been those of six-membered rings. ${ }^{10,11}$ We have undertaken theoretical studies of low-valent $\mathrm{Al}-\mathrm{P}$ compounds, both unassociated ${ }^{12}$ and now ring and cluster compounds. We report here theoretical structures, energies, and vibrational frequencies for the $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring, which contains three coordinate aluminum and phosphorus, and the $\left(\mathrm{H}_{2} \mathrm{Al}-\right.$ $\left.\mathrm{PH}_{2}\right)_{2}$ ring and the $(\mathrm{HAl}-\mathrm{PH})_{4}$ cluster, which contain four coordinate atoms.

## Theoretical Methods

$A b$ initio theoretical studies were carried out initially at the Hartree-Fock self-consistent-field (SCF) level, using a double- $\zeta$ plus polarization (DZP) basis set. The Huzinaga-Dunning (4s/ 2s) basis set was used for hydrogen, ${ }^{13,14}$ and the HuzinagaDunning ( $11 \mathrm{~s} 7 \mathrm{p} / 6 \mathrm{~s} 4 \mathrm{p}$ ) basis set was used for aluminum and phosphorus. ${ }^{15,16}$ The exponents for the polarization functions were $\mathrm{Al}=0.40, \mathrm{P}=0.80$, and $\mathrm{H}=0.75$. Electron correlation was included via the method of configuration interaction including all single and double excitations (CISD) and the coupled cluster method including all single and double excitations (CCSD). In all correlated methods the orbitals corresponding to the Al and P 1s atomic orbitals were frozen, and the corresponding high-energy virtual orbitals deleted. A larger basis set was also used to assure that no anomalous results were obtained due to small basis set size. Triple- $\zeta$ plus double polarization (TZ2P) basis sets consisting of the HuzinagaDunning ${ }^{13,17}(5 \mathrm{~s} / 3 \mathrm{~s})$ basis set on hydrogen and the McLeanChandler ( $12 \mathrm{~s} 9 \mathrm{p} / 6 \mathrm{~s} 5 \mathrm{p}$ ) basis set on aluminum and phosphorus were used. ${ }^{15,18}$ The exponents of the TZ2P polarization functions were $\mathrm{H}=(1.50,0.375), \mathrm{P}=(1.20,0.30), \mathrm{Al}=(0.80$, 0.20 ). Geometry optimizations were performed via analytic


Figure 1. Theoretical geometry of the cis-puckered $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring in angstroms and degrees.


Figure 2. Theoretical geometry of the trans-puckered $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring in angstroms and degrees.
first-derivative methods. Harmonic vibrational frequencies were obtained via analytic second derivatives at the Hartree-Fock level. The PSI suite of programs was used throughout. ${ }^{19}$

## Results and Discussion

The theoretical geometries of the three-coordinate (HAl$\mathrm{PH})_{2}$ ring in different conformations are given in Figures 1 and 2. The harmonic vibrational frequencies are given in Tables 1 and 2. The theoretical geometry of the four-coordinate $\left(\mathrm{H}_{2}-\right.$ $\left.\mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring is given in Figure 3, and the corresponding predicted harmonic vibrational frequencies are given in Table 3. The results for the cube are given in Figure 4 and Table 4. We will discuss first the geometries and harmonic vibrational frequencies of the two rings and the cube in turn, and then we will examine the energies of the reactions that lead to formation of the cube from an initial $\mathrm{H}_{3} \mathrm{Al}-\mathrm{PH}_{3}$ adduct.
$(\mathbf{H A l}-\mathbf{P H})_{2}$. One might expect, on the basis of the structure of the six-membered ring of Wehmschulte and Power, ${ }^{2}$ that this four-membered $\mathrm{Al}-\mathrm{P}$ ring would be puckered. Puckering of the ring creates two possible orientations for the hydrogen attached to phosphorus, similar to the axial and equatorial sites of cyclohexane, although the difference between axial and equatorial is smaller in the four-membered ring than in cyclohexane, because the degree of puckering is smaller. There are three possible conformations: axial hydrogens at both phosphorus atoms, equatorial at both, or an axial-equatorial mix. Geometry optimizations at the DZP SCF level were begun from each of these conformations. No stationary point was found for the axial-axial conformation. The optimization that was begun at the axial-axial arrangement underwent ring inversion

TABLE 1: SCF Vibrational Frequencies in $\mathrm{cm}^{-1}$ and Infrared Intensities in $\mathrm{km} \mathrm{mol}^{-1}$ (in Parentheses) for the cis-Puckered Conformation of the (HAl-PH) $\mathbf{R H}^{\text {Ring }}{ }^{a}$

| mode (intensity) | DZP | TZ2P |
| :--- | ---: | ---: |
| $\mathrm{A}_{1}$ |  |  |
| P-H str. (6) | 2578 | 2529 |
| Al-H str. (47) | 2046 | 2033 |
| P-H wag (28) | 609 | 598 |
| Al-H wag (141) | 466 | 462 |
| Al-P str. (3) | 454 | 454 |
| ring angle def (216) | 216 | 224 |
| ring pucker (0) | 146 | 139 |
| A $_{2}$ |  |  |
| Al-P-H bend (0) | 639 | 616 |
| P-Al-H bend (0) | 560 | 545 |
| Al-P str. (0) | 395 | 374 |
| B $_{1}$ P-H str. (57) | 2578 | 2529 |
| P-Al-H bend (414) | 686 | 677 |
| P-Al-H + P-H wag (3) | 478 | 463 |
| P inversion (113) | 191 | 193 |
| B $_{2}$ |  |  |
| Al-H str. (462) | 2041 | 2027 |
| Al-P-H bend (0) | 764 | 737 |
| Al-H wag (92) | 448 | 447 |
| Al-P str. (2) | 414 | 392 |

${ }^{a}$ Intensities were obtained at the DZP SCF level.
TABLE 2: SCF Vibrational Frequencies in $\mathrm{cm}^{-1}$ and Infrared Intensities in $\mathrm{km} \mathrm{mol}^{-1}$ (in Parentheses) for the trans-Planar Conformation of the $(\mathbf{H A l}-\mathbf{P H})_{2}$ Ring $^{a}$

| mode (intensity) | DZP | TZ2P |
| :--- | ---: | ---: |
| $\mathrm{A}_{\mathrm{g}}$ P-H str. (0) |  |  |
| Al-H str. (0) | 2599 | 2551 |
| P-H wag (0) | 576 | 2033 |
| Al-P str. (0) | 547 |  |
| ring angle def. (0) | 210 | 425 |
| $\mathrm{~A}_{\mathrm{u}}$ |  | 197 |
| Al-H str. (519) | 2045 | 2027 |
| Al-P-H bend (7) | 711 | 694 |
| Al-P str. (67) | 443 | 427 |
| $\mathrm{~B}_{\mathrm{g}}$ Al-P-H bend (0) | 729 | 712 |
| P-Al-H bend (0) | 584 | 581 |
| Al-H wag (0) | 465 | 455 |
| Al-P str. (0) | 413 | 395 |
| $\mathrm{~B}_{\mathrm{u}}$ |  |  |
| P-H str. (75) | 2599 | 2551 |
| P-Al-H bend (405) | 699 | 679 |
| Al-H wag (139) | 505 | 498 |
| P-H, Al-H bend comb. (139) | 447 | 441 |
| P inversion (48) | 210 | 232 |
| ring pucker (24) | 99 | 55 |

${ }^{a}$ Intensities were obtained at the DZP SCF level.
to the equatorial-equatorial conformation. The optimization begun with an equatorial-axial conformation converges to a minimum on the potential surface for which the ring is planar. We shall refer to it as the trans-planar conformation, and it has $C_{2 h}$ symmetry and a ${ }^{1} \mathrm{~A}_{g}$ ground state. The equatorialequatorial conformation has $C_{2 v}$ symmetry and a ${ }^{1} \mathrm{~A}_{1}$ ground state. We will refer to the equatorial-equatorial conformation as cis-puckered. The cis-puckered ring lies only $0.4 \mathrm{kcal} \mathrm{mol}^{-1}$ below the trans-planar conformation at the DZP SCF level. Both increase in basis set size and correlated levels of theory favor the cis-puckered conformation. The cis-puckered ring is lower in energy by $2.2 \mathrm{kcal} \mathrm{mol}^{-1}$ at the TZ2P SCF level, and at the DZP CCSD level it is $1.5 \mathrm{kcal} \mathrm{mol}^{-1}$ lower in energy. If we assume the effects of basis set and correlation are additive, we estimate that the cis-puckered ring is about $3 \mathrm{kcal} \mathrm{mol}^{-1}$ lower than the trans-planar ring in energy.


Figure 3. Theoretical geometry of the $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring in angstroms and degrees.

TABLE 3: SCF Vibrational Frequencies in $\mathrm{cm}^{-1}$ and Infrared Intensities in $\mathrm{km} \mathrm{mol}^{-1}$ (in Parentheses) for the $\left(\mathbf{H}_{2} \mathrm{Al}-\mathbf{P H}_{2}\right)_{2}$ Ring $^{\boldsymbol{a}}$

| mode (intensity) | DZP | TZ2P |
| :---: | :---: | :---: |
| Ag |  |  |
| $\mathrm{P}-\mathrm{H}$ str. (0) | 2618 | 2587 |
| $\mathrm{Al}-\mathrm{H}$ str. (0) | 2011 | 1981 |
| $\mathrm{H}-\mathrm{P}-\mathrm{H}$ bend (0) | 1183 | 1193 |
| $\mathrm{H}-\mathrm{Al}-\mathrm{H}$ bend (0) | 797 | 786 |
| $\mathrm{Al}-\mathrm{P}$ str. (0) | 355 | 352 |
| ring angle def. (0) | 226 | 210 |
| $\mathrm{B}_{1 \mathrm{~g}}$ |  |  |
| $\mathrm{AlH}_{2}$ wag (0) | 659 | 646 |
| $\mathrm{PH}_{2}$ wag (0) | 595 | 596 |
| ring angle def. (0) | 275 | 268 |
| $\mathrm{B}_{2 \mathrm{~g}}$ |  |  |
| $\mathrm{P}-\mathrm{H}$ str. (0) | 2627 | 2594 |
| $\mathrm{AlH}_{2}$ twist (0) | 547 | 541 |
| $\mathrm{PH}_{2}$ rock (0) | 290 | 302 |
| $\mathrm{B}_{3 \mathrm{~g}}$ |  |  |
| $\mathrm{Al}-\mathrm{H}$ str. (0) | 2013 | 1984 |
| $\mathrm{PH}_{2}$ str. (0) | 733 | 736 |
| $\mathrm{AlH}_{2}$ rock (0) | 289 | 284 |
| $\mathrm{A}_{u}$ |  |  |
| $\mathrm{PH}_{2}$ twist (0) | 712 | 709 |
| $\mathrm{AlH}_{2}$ twist (0) | 422 | 412 |
| $\mathrm{B}_{1 \mathrm{u}}$ |  |  |
| $\mathrm{P}-\mathrm{H}$ str. (20) | 2627 | 2594 |
| $\mathrm{Al}-\mathrm{H}$ str. (448) | 2015 | 1984 |
| $\mathrm{AlH}_{2}$ rock (57) | 512 | 512 |
| $\mathrm{PH}_{2}$ rock (25) | 291 | 301 |
| ring pucker (6) | 27 | 25 |
| $\mathrm{B}_{2 \mathrm{u}}$ |  |  |
| Al-H str. (303) | 2005 | 1977 |
| $\mathrm{H}-\mathrm{Al}-\mathrm{H}$ bend (689) | 792 | 786 |
| $\mathrm{PH}_{2}$ wag (110) | 658 | 662 |
| Al-P str. (25) | 347 | 346 |
| $\mathrm{B}_{3 \mathrm{u}}$ |  |  |
| $\mathrm{P}-\mathrm{H}$ str. (31) | 2616 | 2584 |
| $\mathrm{H}-\mathrm{P}-\mathrm{H}$ str. (78) | 1160 | 1171 |
| $\mathrm{AlH}_{2}$ wag (799) | 743 | 729 |
| $\mathrm{Al}-\mathrm{P}$ str. (26) | 319 | 321 |

${ }^{a}$ Intensities were obtained at the DZP SCF level.
The $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring has nondative bonds between three coordinate Al and P. As mentioned above, Haaland used the Schomaker-Stevenson rule to estimate a bond length of 2.31 $\AA$ for these bonds, ${ }^{4}$ and the $\mathrm{Al}-\mathrm{P}$ bond length obtianed by X-ray crystallography for the two known compounds are 2.328(3) $\AA$ for the six-membered ring $^{2}$ and 2.342(2) $\AA$ for the unassociated compound. ${ }^{3}$ At the DZP CCSD level we obtain at $\mathrm{Al}-\mathrm{P}$ bond length of $2.298 \AA$ for the cis-puckered ring and $2.288 \AA$ for the trans-bent. At the SCF level an increase in basis set size from DZP to TZ2P causes a lengthening of the $\mathrm{Al}-\mathrm{P}$ bond for both conformations. If we assume additivity for changes in bond length due to basis set and correlation effects, the theoretical


Figure 4. DZP SCF theoretical geometry of the $(\mathrm{HAl}-\mathrm{PH})_{4}$ cube in angstroms and degrees.
TABLE 4: DZP SCF Vibrational Frequencies in $\mathrm{cm}^{-1}$ and Infrared Intensities in $\mathbf{k m ~ m o l}^{-1}$ (in Parentheses) for the $(\mathbf{H A l}-\mathrm{PH})_{4}$ Cube $^{a}$

| mode (intensity) | frequency |
| :---: | :---: |
| $\mathrm{A}_{1}$ |  |
| $\mathrm{P}-\mathrm{H}$ str. (0) | 2620 |
| $\mathrm{Al}-\mathrm{H}$ str. (0) | 2036 |
| $\mathrm{Al}-\mathrm{P}$ str. (0) | 400 |
| cube angle def. (0) | 338 |
| E |  |
| $\mathrm{P}-\mathrm{H}$ bend (0) | 617 |
| $\mathrm{Al}-\mathrm{H}$ bend (0) | 542 |
| $\mathrm{Al}-\mathrm{P}$ str. (0) | 318 |
| cube angle def. (0) | 177 |
| $\mathrm{~T}_{1}$ |  |
| $\mathrm{P}-\mathrm{H}$ bend (0) | 563 |
| Al-H bend (0) | 485 |
| Al-P str. (0) | 304 |
| $\mathrm{~T}_{2}$ | 2627 |
| $\mathrm{P}-\mathrm{H}$ str. (37) | 2031 |
| Al-H str. (1084) | 677 |
| $\mathrm{P}-\mathrm{H}$ bend (361) | 631 |
| Al-H bend (1104) | 396 |
| Al-P str. (90) | 360 |
| Al-P str. (33) | 174 |
| cube angle def. (1) |  |

${ }^{a}$ Intensities were obtained at the DZP SCF level.
value that we obtain for the $\mathrm{Al}-\mathrm{P}$ bond is $2.313 \AA$ for the cispuckered conformation and $2.301 \AA$ for the trans-bent. The agreement between model compound and experiment is remarkable if one considers the difference between the hydrogen atom of the model and the sterically demanding groups of the compounds synthesized. The bond length obtained by Matsunaga and Gordon for the six-membered-ring model compound $(\mathrm{HAl}-\mathrm{PH})_{3}$ was $2.315 \AA$ at the SCF level using effective core potentials for Al and $\mathrm{P} .{ }^{11}$ The $\mathrm{Al}-\mathrm{P}$ bond in the unassociated model compound $\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}$ is 2.309 at the DZP CCSD level, slightly longer than those of the $(\mathrm{HAl}-\mathrm{PH})_{2}$ four-memberedring conformers at the DZP CCSD level. The $\mathrm{Al}-\mathrm{P}$ bond length is seen to be very stable with respect to changes in its steric environment. The consistency of the $\mathrm{Al}-\mathrm{P}$ bond length implies that there is little change in the hybridization of the orbitals on Al and P whether the molecule is the unassociated $\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}$, the four-membered ring, or the six-membered ring.

In contrast to the $\mathrm{Al}-\mathrm{P}$ bond lengths, the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angles differ sharply between the values found experimentally for the six-membered ring and the theoretical values in the model $(\mathrm{HAl}-\mathrm{PH})_{2}$ four-membered ring. The experimental $\mathrm{Al}-\mathrm{P}-$ Al angle ${ }^{2}$ in the six-membered ring has an average value of
$111^{\circ}$, but the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angle in our four-membered ring is $75.4^{\circ}$ (cis-puckered, CCSD DZP level), a decrease of about $35^{\circ}$. The $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angle in the six-membered ring has an average experimental value of $112^{\circ}$, compared to the theoretical value of $94.7^{\circ}$ (cis-puckered, CCSD DZP), a decrease of about $17^{\circ}$. Of course the simple geometric constraint of closing a fourmembered ring will cause a decrease in the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ and $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angles, but one wonders why the angle change at phosphorus is double that at aluminum. If, however, we assume that a normal bond angle about a three coordinate phosphorus is about $95^{\circ}$ and a normal bond angle about a three coordinate aluminum is $120^{\circ}$, then the angles in the four-membered ring are a reasonable compromise: the angle at phosphorus narrows by about $20^{\circ}$, from a normal angle of $95^{\circ}$ to an angle of $75^{\circ}$, and the angle at aluminum narrows by $25^{\circ}$, from a normal angle of $120^{\circ}$ to $95^{\circ}$.

The ring stretching vibrational frequencies are in the range $390-450 \mathrm{~cm}^{-1}$. This range brackets the $432 \mathrm{~cm}^{-1}$ value predicted theoretically for the $\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}$ compound. The ring butterfly motion is the cis-puckered conformer has a frequency of $140 \mathrm{~cm}^{-1}$ (TZ2P SCF); the same motion has a much smaller frequency, only $55 \mathrm{~cm}^{-1}$, in the trans-bent conformer. This is substantially smaller than the value of $233 \mathrm{~cm}^{-1}$ obtained for the butterfly motion of the analogous $\mathrm{Al}-\mathrm{N}$ ring, $(\mathrm{HAl}-\mathrm{NH})_{2} .^{20}$
$\left(\mathbf{H}_{\mathbf{2}} \mathbf{A l}-\mathbf{P H}_{2}\right)_{\mathbf{2}}$. The $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}\right)_{2}$ four coordinate ring is planar, but the frequency of the butterfly motion is very low, only $26 \mathrm{~cm}^{-1}$ at the DZP SCF level, and $25 \mathrm{~cm}^{-1}$ at the TZ2P SCF level. For the analogous $\mathrm{Al}-\mathrm{N}$ ring, electron correlation had little effect on the frequencies of the butterfly motion, and as correlation does not drastically change the geometry of the ring, we therefore would expect correlation would not dramatically decrease the floppiness of the $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring. The decrease in the frequency for the butterfly motion from ( $\mathrm{HAl}-$ $\mathrm{PH})_{2}$ to $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ could be predicted on the basis of the change in the $\mathrm{Al}-\mathrm{P}$ bonds between the two rings. As Haaland has pointed out, ${ }^{4}$ for $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ the $\mathrm{Al}-\mathrm{P}$ bonds can be viewed as half dative and half "normal" (i.e. nondative). Our theoretical estimate of the $\mathrm{Al}-\mathrm{P}$ bond length in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ is $2.451 \AA$, on the basis of the DZP CCSD value of $2.438 \AA$ plus $\Delta r=0.013 \AA$, which is the TZ2P SCF - DZP SCF difference. This value is nearly identical to that obtained for the four-membered $\left(\mathrm{R}_{2} \mathrm{Al}-\mathrm{PR}^{\prime}\right)_{2}$ ring $\left(\mathrm{R}=\mathrm{SiMe}_{3}, \mathrm{R}^{\prime}=\right.$ cyclohexyl) reported experimentally by Janik, Duesler, McNamara, Westerhausen, and Paine. ${ }^{21}$ They found $\mathrm{Al}-\mathrm{P}$ bond lengths of $2.45 \AA$ and $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angles of $94^{\circ}$. The $\mathrm{Al}-\mathrm{P}$ bond length in the six-membered ring composed of four coordinate Al and P , $\left(\mathrm{Me}_{2} \mathrm{Al}-\mathrm{PMe}_{2}\right)_{3}$, is $2.43 \AA .{ }^{22}$ The value given for half dative/half normal bonds by Haaland ${ }^{4}$ was $2.43 \AA$. Once again the $\mathrm{Al}-\mathrm{P}$ bond length is very consistent among theoretical predictions and different experimentally determined values.

At first glance the bond angles in the four-membered $\left(\mathrm{H}_{2}-\right.$ $\left.\mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring might be puzzling. In contrast to the ( $\mathrm{HAl}-$ $\mathrm{PH})_{2}$ ring, the angle at phosphorus in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ is wider than the angle at aluminum. The $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angle is $96.0^{\circ}$ at the DZP CCSD level, and the $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angle is $84.0^{\circ}$. This result is consistent with experiment. In the $\left(\mathrm{R}_{2} \mathrm{Al}-\mathrm{PR}^{\prime}\right)_{2}$ ring reported by Janik et al. ${ }^{21}$ the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angle is $94^{\circ}$, while the $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angle is $86^{\circ}$. To understand why the angle at phosphorus opens in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ compared to $(\mathrm{HAl}-\mathrm{PH})_{2}$, we again consider the orbitals used for ring bonding. As shown in Figure 5b, the saturated ring has a mixture of dative and nondative bonds. For aluminum, the orbitals used in ring bonding are an $\mathrm{sp}^{2}$ hybrid and the empty p orbital, and the angle between them is $90^{\circ}$. For phosphorus the orbitals used in ring bonding are a weakly hybridized s lone pair and p bonding


Figure 5. Bond angles between (a) two normal covalent bonds and (b) a dative bond and a normal covalent bond.
orbitals. (There is some $s-p$ hybridization in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$, because the $\mathrm{H}-\mathrm{P}-\mathrm{H}$ angles are $100.4^{\circ}$ at the DZP CCSD level, rather than $90^{\circ}$.) The angle between the lone pair and the p orbital is approximately $120^{\circ}$. If the phosphorus angle remained unchanged, the angle at Al would have to be $60^{\circ}$ in a planar four-membered ring; if the angle at Al remained unchanged, the angle at P would have to drop from $120^{\circ}$ to $90^{\circ}$. The ring angles are therefore again a compromise, but in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ the compromise is achieved by a decrease in the angle at phosphorus from $\sim 120^{\circ}$ to $96^{\circ}$ and a decrease at aluminum from $90^{\circ}$ to $84^{\circ}$. Experimental results on the nonplanar six-membered $\left(\mathrm{Me}_{2} \mathrm{Al}-\mathrm{PMe}_{2}\right)_{3}$ ring, for which there is less angle constraint, find the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angle to be $120.4^{\circ}$ and the $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angle to be only $99^{\circ} .{ }^{22}$
$(\mathbf{H A l}-\mathbf{P H})_{4}$. This cubic cluster was studied at the DZP SCF level. We may compare the results obtained at the DZP SCF level with the results at higher levels of theory for $(\mathrm{HAl}-\mathrm{PH})_{2}$ and $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ to estimate the reliability of the DZP SCF results. For the $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring, we find that the $\mathrm{Al}-\mathrm{P}$ bond length is overestimated by about $0.02 \AA$ at the DZP SCF level compared to our best estimates. The other geometrical parameters have smaller errors. For the cubic cluster the $\mathrm{Al}-\mathrm{P}$ bond length is $2.434 \AA$, and we would assume on the basis of earlier results that this is an upper limit to the bondlength that would be obtained at higher levels of theory, which are likely to be 0.01 to $0.02 \AA$ shorter. The $\mathrm{Al}-\mathrm{P}$ bond length determined by X-ray crystallography for the substituted cube synthesized by Cowley et al. is $2.414(4) \AA$ (av). ${ }^{1}$ The steric demands of the bulky groups on Al and P do not appear to affect the $\mathrm{Al}-\mathrm{P}$ bond length. As was the case for $\mathrm{Al}-\mathrm{N}$ compounds, the bonds in the cube are shorter than those of the saturated four-membered ring, but longer than the unsaturated four-membered ring. ${ }^{20}$ This is consistent with Haaland's analysis ${ }^{4}$ that in the $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring the $\mathrm{Al}-\mathrm{P}$ bonds are not dative, in the cube they can be seen as one-third dative, two-thirds normal, and in the $\left(\mathrm{H}_{2} \mathrm{Al}-\right.$ $\left.\mathrm{PH}_{2}\right)_{2}$ ring, they can be seen as half normal and half dative.

For the $(\mathrm{HAl}-\mathrm{PH})_{4}$ cube the $\mathrm{Al}-\mathrm{P}-\mathrm{Al}$ angle is $91.4^{\circ}$ and the $\mathrm{P}-\mathrm{Al}-\mathrm{P}$ angle is $88.6^{\circ}$ at the DZP SCF level. This is opposite the experimental results. The crystal structure of the cube has an angle at P of $88.2^{\circ}$ and an angle at Al of $91.8^{\circ}$. However, this reversal is only a difference of about $2.5^{\circ}$ and could be due to the presence of substituents in the structure determined by crystallography.

The lowest frequency vibration is the cube angle deformation at $147 \mathrm{~cm}^{-1}$. The $\mathrm{Al}-\mathrm{P}$ stretching modes in the cube are clustered around $400 \mathrm{~cm}^{-1}$. They are lower than the ring modes of $(\mathrm{HAl}-\mathrm{PH})_{2}$, the highest of which is $478 \mathrm{~cm}^{-1}$, and higher than those found in $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$, for which the highest $\mathrm{Al}-\mathrm{P}$ stretch is $352 \mathrm{~cm}^{-1}$.

Reaction Energies. A model reaction sequence for synthesis of the $\mathrm{Al}-\mathrm{P}$ cubic cluster may be constructed as

$$
\begin{gather*}
\mathrm{H}_{3} \mathrm{Al}-\mathrm{PH}_{3} \rightarrow \mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}+\mathrm{H}_{2} \quad \text { (dehydrogenation) } \\
2\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right) \rightarrow\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2} \quad \text { (ring formation) } \\
\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2} \rightarrow(\mathrm{HAl}-\mathrm{PH})_{2}+2 \mathrm{H}_{2} \quad \text { (dehydrogenation) }  \tag{2a}\\
2(\mathrm{HAl}-\mathrm{PH})_{2} \rightarrow(\mathrm{HAl}-\mathrm{PH})_{4} \quad \text { (cube formation) } \tag{2b}
\end{gather*}
$$

We can assess the energy required to carry out these reactions in this completely stepwise (nonconcerted) fashion. Early work by Beachley, Coates, and Koonstan ${ }^{24}$ indicated that the analogous reactions for $\mathrm{Al}-\mathrm{N}$ compounds do not take place by this simple mechanism. Our results provide thermodynamic parameters for the concerted mechanism and thus upper limits for other mechanisms. They also provide estimates of bond energies for $\sigma$ and $\pi \mathrm{Al}-\mathrm{P}$ bonds. We have determined in a separate study of $\mathrm{Al}-\mathrm{P}$ compounds that the energy of step 1a is $8.3 \mathrm{kcal} \mathrm{mol}^{-1}, 3.3 \mathrm{kcal} \mathrm{mol}^{-1}$ if zero point vibrational energy (ZPVE) is included. ${ }^{12}$ For all energy difference calculations, ZPVE is determined using unscaled DZP SCF vibrational frequencies. Dimerization of the resulting $\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}$ monomer (reaction 1b) has a $\Delta E$ value of $-34.1 \mathrm{kcal} \mathrm{mol}^{-1}$ at the DZP SCF level and -34.3 at the TZ2P SCF level. The small variation with basis set size is consistent with a lack of significant basis set superposition (BSSE) error. Including electron correlation gives a value of $-38.9 \mathrm{kcal} \mathrm{mol}^{-1}$ at the DZP CCSD, $-36.0 \mathrm{kcal} \mathrm{mol}^{-1}$ including ZPVE correction. The overall energy change for step 1 at the DZP CCSD level is $-30.6 \mathrm{kcal} \mathrm{mol}^{-1}$ ( -32.7 with ZPVE corrections). This large negative value is consistent with initial ring formation in the synthesis of the cube occuring at low temperature. ${ }^{1}$

As the $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring is formed in step 1 b , the Al and P atoms become four coordinate by forming two $\sigma$ dative bonds. If we divide the total energy change for dimerization in half, we obtain a value of $15.3 \mathrm{kcal} \mathrm{mol}^{-1}$ per bond formed in the ring. Estimates for $\Delta E$ values for the $\sigma$ dative bond between $\mathrm{AlH}_{3}$ and $\mathrm{PH}_{3}$ range from 13.2 to $15.2 \mathrm{kcal} \mathrm{mol}^{-1}$ (without ZPVE or BSSE corrections). The best value from the earlier $\mathrm{AlH}_{3}-\mathrm{PH}_{3}$ study ${ }^{12}$ was $13.6 \mathrm{kcal} \mathrm{mol}{ }^{-1}$ at the TZ2P CCSD level, but if we compare at identical levels of theory, namely, DZP CCSD, the value was $12.5 \mathrm{kcal} \mathrm{mol}^{-1}$. Thus dative bond formation in the ring is more favorable energetically by 2.8 kcal $\mathrm{mol}^{-1}$ at the DZP CCSD level than the simple $\mathrm{AlH}_{3}-\mathrm{PH}_{3}$ dative bond.

In the synthesis ${ }^{1}$ of the $\mathrm{Al}-\mathrm{P}$ cube, initial alkane loss to form a four-membered ring proceeded at $25^{\circ} \mathrm{C}$, but loss of alkane from that ring accompanied melting at $80^{\circ} \mathrm{C}$. We would therefore expect that $\mathrm{H}_{2}$ loss from the $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring (step 2a) would require more energy than the $\mathrm{H}_{2}$ loss in step 1a. At the DZP CCSD level, the energy required for step 2a is 39.2 $\mathrm{kcal} \mathrm{mol}{ }^{-1}$ ( 31.3 including ZPVE). The DZP SCF and TZ2P SCF values are 41.7 and $36.4 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively. For this reaction the extension of the basis set results in a 5.3 kcal $\mathrm{mol}^{-1}$ change in $\Delta E$. We estimate the reaction energy to be $39.2 \mathrm{kcal} \mathrm{mol}^{-1}$ (DZP CCSD) - $5.3 \mathrm{kcal} \mathrm{mol}^{-1}$ (TZ2P correction) $=33.9$, or approximately $34 \mathrm{kcal} \mathrm{mol}^{-1}$. Including ZPVE corrections drops this value to $26 \mathrm{kcal} \mathrm{mol}^{-1}$, which is substantially lower than that found for the same reaction in the analogous $\mathrm{Al}-\mathrm{N}$ rings, $43 \mathrm{kcal} \mathrm{mol}{ }^{-1} .{ }^{20}$

Dimerization of ( $\mathrm{HAl}-\mathrm{PH})_{2}$ to form the cube (step 2b) has a $\Delta E$ value of $-68.1 \mathrm{kcal} \mathrm{mol}^{-1}\left(-65.3 \mathrm{kcal} \mathrm{mol}^{-1}\right.$ including ZPVE). This value is also substantially smaller (in absolute value) than that obtained for the analogous $\mathrm{Al}-\mathrm{N}$ system, -112 kcal $\mathrm{mol}^{-1} .{ }^{20}$ The overall energy for step 2 is estimated to be
$-34 \mathrm{kcal} \mathrm{mol}^{-1}$ ( $-39 \mathrm{kcal} \mathrm{mol}^{-1}$ including ZPVE), which is somewhat larger than the overall energy of $-27 \mathrm{kcal} \mathrm{mol}^{-1}$ for the same reaction in the $\mathrm{Al}-\mathrm{N}$ system. The major difference between the $\mathrm{Al}-\mathrm{N}$ and the $\mathrm{Al}-\mathrm{P}$ reactions is thus the relatively greater stability of the $\mathrm{Al}-\mathrm{P}$ intermediate $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring.

## Conclusions

The overall shape of the rings and the bond lengths and angles are consistent with the simple understanding of bonds as being dative, nondative, or a mixture, as elaborated by Haaland. ${ }^{4}$ The unknown $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring is predicted here to be puckered in the lowest energy configuration, but a planar geometry is nearly isoenergetic. The small bond angles at phosphorus and large angles at aluminum in this ring are due to the $120^{\circ}$ angles between $\mathrm{sp}^{2}$ orbitals on Al and the $90^{\circ}$ angles between p orbital bonds on P . The bonds in this ring are also shorter than those of the cube or the saturated ring, because they are completely nondative. The $\mathrm{Al}-\mathrm{P}$ bond length is longest in the $\left(\mathrm{H}_{2} \mathrm{Al}-\right.$ $\left.\mathrm{PH}_{2}\right)_{2}$ ring, for which the bonds are half dative and half nondative. Compared to the $\mathrm{Al}-\mathrm{N}$ analogs, the unsaturated four-membered $(\mathrm{HAl}-\mathrm{PH})_{2}$ ring is lower in energy relative to the saturated $\left(\mathrm{H}_{2} \mathrm{Al}-\mathrm{PH}_{2}\right)_{2}$ ring. Four-membered rings with three coordinate Al and N have been synthesized, ${ }^{3,23}$ and one would expect that, on the basis of thermodynamic considerations, an $\left(\mathrm{RAl}-\mathrm{PR}^{\prime}\right)_{2}$ ring should also be achievable in the laboratory. The overall energetics of cube formation are similar for the $\mathrm{Al}-\mathrm{N}$ and $\mathrm{Al}-\mathrm{P}$ synthesis, with the results for $\mathrm{Al}-\mathrm{P}$ being consistent with formation of the cube under milder conditions than those required for the $\mathrm{Al}-\mathrm{N}$ cube.

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